## Lecture Notes I - (Discrete) Sample spaces and the Multinomial

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Sample space, outcome, event, probability,...

Discrete sample spaces

Repeated independent trials, Binomial, Multinomial

Reading: Ch. 2, 3

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## Basic vocabulary

- ► *S* sample space (outcome space)
- $\triangleright$   $x \in S$  outcome
- $E \subseteq S$  event  $2^S = \{E \mid E \subseteq S\} \equiv \mathcal{P}(S)$
- $\blacktriangleright P: 2^{S} \rightarrow [0,1] \text{ probability}$ distribution
- $f: S \rightarrow \mathbb{R}$  random variable
- $f: S \rightarrow \mathbb{R}$  statistic

#### Discrete sample spaces



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## Repeated independent trials, Binomial, Multinomial

A coin is tossed 4 times, and the probability of 1 is p > 0.5. The outcomes, their probability and their counts are (in order of decreasing probability):

outcome x	<i>n</i> 0	<i>n</i> <sub>1</sub>	P(x)	event
1111	0	4	$p^4$	E <sub>0,4</sub>
1110	1	3	$p^{3}(1-p)^{1}$	E <sub>1,3</sub>
1101	1	3	$p^{3}(1-p)^{1}$	
1011	1	3	$p^{3}(1-p)^{1}$	
0111	1	3	$p^{3}(1-p)^{1}$	
1100	2	2	$p^2(1-p)^2$	E <sub>2,2</sub>
1010	2	2	$p^2(1-p)^2$	
1001	2	2	$p^2(1-p)^2$	
0110	2	2	$p^2(1-p)^2$	
0101	2	2	$p^2(1-p)^2$	
0011	2	2	$p^2(1-p)^2$	
0100	3	1	$p^1(1-p)^3$	E <sub>3,1</sub>
1000	3	1	$p^1(1-p)^3$	
0010	3	1	$p^1(1-p)^3$	
0001	3	1	$p^1(1-p)^3$	
0000	4	0	$(1-p)^4$	E <sub>4,0</sub>

## Repeated independent trials, Binomial, Multinomial

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