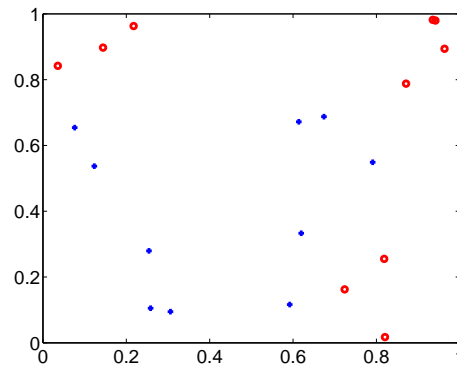


STAT 535 Homework 1  
Out October 8, 2020  
Due October 15, 2020  
©Marina Meilă  
mmp@stat.washington.edu

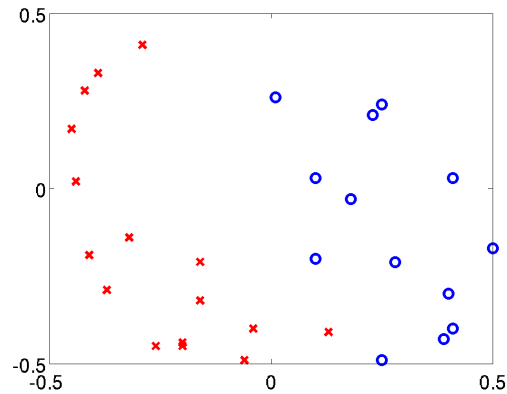
**Problem 1 – Decision regions**

- a. Draw a reasonable decision tree for the following data (i.e. perform the algorithm “by hand”).



*The data and file are provided on the Assignments web page.*

- b. Make a plot of the decision regions of the 1-NN classifiers for the same data.
- c. Make a plot of the decision regions of the 3-NN classifiers for the same data. (*Make a plot as good as you can by hand*)
- d. Draw an approximate plot of the decision region that LDA would obtain on the data below (next page). Show the means of the two classes on the plot.
- e. Draw an approximate plot of the decision region that QDA would obtain on the data in e.

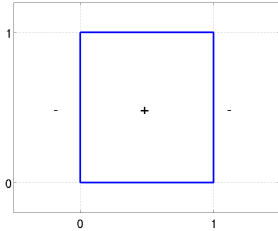


*Note: it is OK to also run a program to do these exercises. But I recommend to first try doing what you can by hand. It would be a better practice for the quiz.*

## Problem 2 – More decision regions

Consider the decision regions below. You will try to obtain this decision boundary with a variety of classifier families, and see if it's possible exactly, approximately, or not at all.

Decision regions



Classifier families

- ☐ decision tree (labeled drawing)
- ☐ decision tree with 2 levels (labeled drawing)
- ☐ 1-NN classifier (labeled drawing of a set of points and locations)
- ☐ 3-NN classifier (labeled drawing of a set of points and locations)
- ☐ Nadaraya-Watson (labeled drawing of a set of points and locations)
- ☐ linear classifier (labeled drawing or formula)
- ☐ quadratic classifier (formula with numerical values or labeled drawing)

More precisely, for each of the predictor classes above

EITHER find a classifier in this class which realizes this decision region exactly

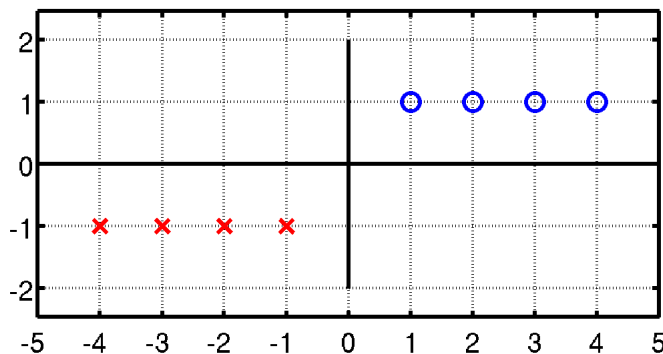
OR find a classifier in this class which approximates this decision region arbitrarily closely; be sure to say which parameter of the classifier controls how accurate is the approximation

OR give a brief argument why it is impossible to approximate this decision region

## Problem 3 – Linear and logistic regression

*Note: it is OK to also run a program to do these exercises. But I recommend to first try doing what you can by hand. It would be a better practice. We grade the answers on the assumptions that you did not have a computer available but that you understood the properties of the regressors.*

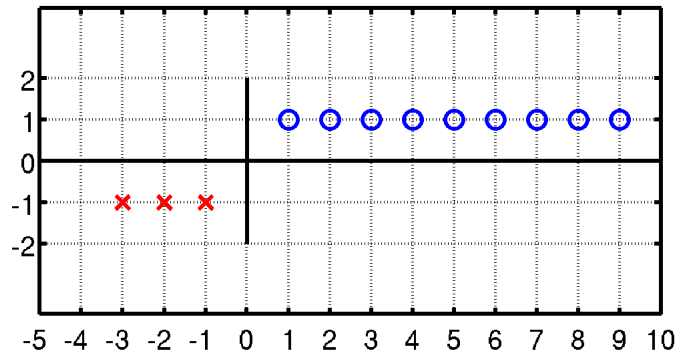
**a.** On the data below, draw approximately  $p(x) = P_{Y=1|X}$  for a logistic regression classifier  $f(x) = \beta x$  with  $\beta = 1$  (see course notes for meaning of  $f$ ).



b. On the same plot, draw approximately  $p(x) = P_{Y=1|X}$  for a logistic regression classifier  $f(x) = \beta x$  with  $\beta = 0.1$ .

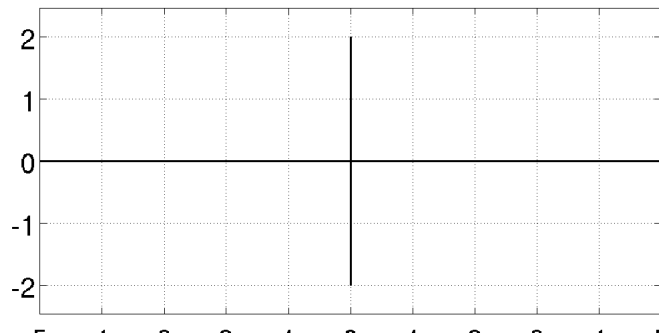
c. Suppose that you have the same data set, but you only have a Linear Regression program available. Draw what a linear regression function  $f(x) = \beta x + \beta_0$  trained on these data will look like. Then mark the decision regions on the  $X$  axis.

d. Given the good experience with Linear Regression in c., you decide to use Linear Regression on the new data set below. Draw what a linear regression function  $f(x) = \beta x + \beta_0$  trained on these data will look like. Then mark the decision regions on the  $X$  axis.



e. Examine the classifier you obtained in d. Does it classify all the examples correctly? Explain in a sentence or two why or why not.

f. Let us return to the data from a. Represent these data points as points in  $\mathbb{R}^2$  of the form  $\tilde{x} = [x \ 1]^T$  on the graph below.



g. On the same graph above, draw the vector  $\beta = [1 \ -1]^T$  and the decision boundary of the linear classifier  $\text{sgn} \beta^T \tilde{x}$ .

**h.** For the data represented as in **f.** draw the centers  $\mu_{\pm}$  and the decision region for the LDA classifier.