



Climate and statistics

Outline

Anomalies

Comparing climate models to data

Downscaling and bias correction

The fit of models

Climate is the distribution of weather

To reasonably estimate a distribution (from data or from models) need a relatively long stretch of data—WMO suggests at least 30 years

How well does the CMIP5 experiment used in the recent IPCC assessment work for describing annual global mean temperature?

The greenhouse effect

Joseph Fourier (1768-1830)
realized that Earth ought to be
a lot cooler than it is.



John Tyndall (1820-1893)
found that water vapor and
CO₂ are greenhouse gases



Svante Arrhenius (1859-1927)
calculated how changes in
CO₂ can heat the planet



A simple climate model

What comes in

$$S\pi r^2(1-a)$$

Solar constant
1365 W/m²

Earth's albedo
0.3

must go out

$$4\pi r^2 \epsilon \sigma T^4$$

Effective emissivity
(greenhouse, clouds)
0.61

Stefan's constant
5.67×10⁻⁸ W/(K⁴·m²)

Solution

$$T^4 = \frac{1365 \times 0.7}{4 \times 0.61 \times 5.67} \times 10^8$$

**Average earth temperature is
T=288K (15°C)**

**One degree Celsius change in
average earth temperature is
obtained by changing
solar constant by 1.4%**

Earth's albedo by 4.5%

effective emissivity by 1.4%

But in reality...

The solar constant is not constant

The albedo changes with land use changes, ice melting and cloudiness

The emissivity changes with greenhouse gas changes and cloudiness

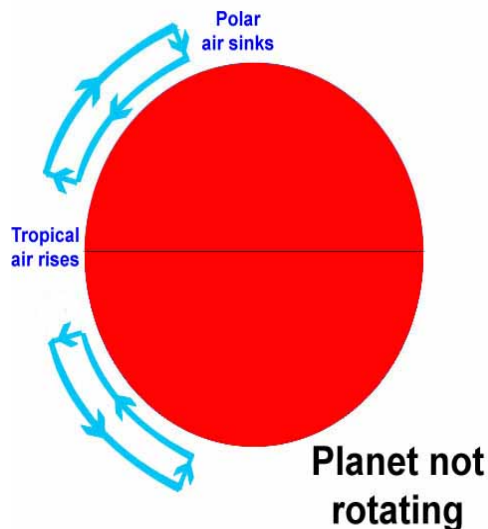
Need to model the three-dimensional (at least) atmosphere

But the atmosphere interacts with land surfaces...

...and with oceans!

The climate engine I

If Earth did not rotate:
tropics get higher solar radiation
hot air rises, reducing surface
pressure
and increasing pressure higher up
forces air towards poles
lower surface pressure at poles
makes air sink
moves back towards tropics



The climate engine II

Since earth does rotate, air packets do not follow longitude lines (Coriolis effect)

Speed of rotation highest at equator

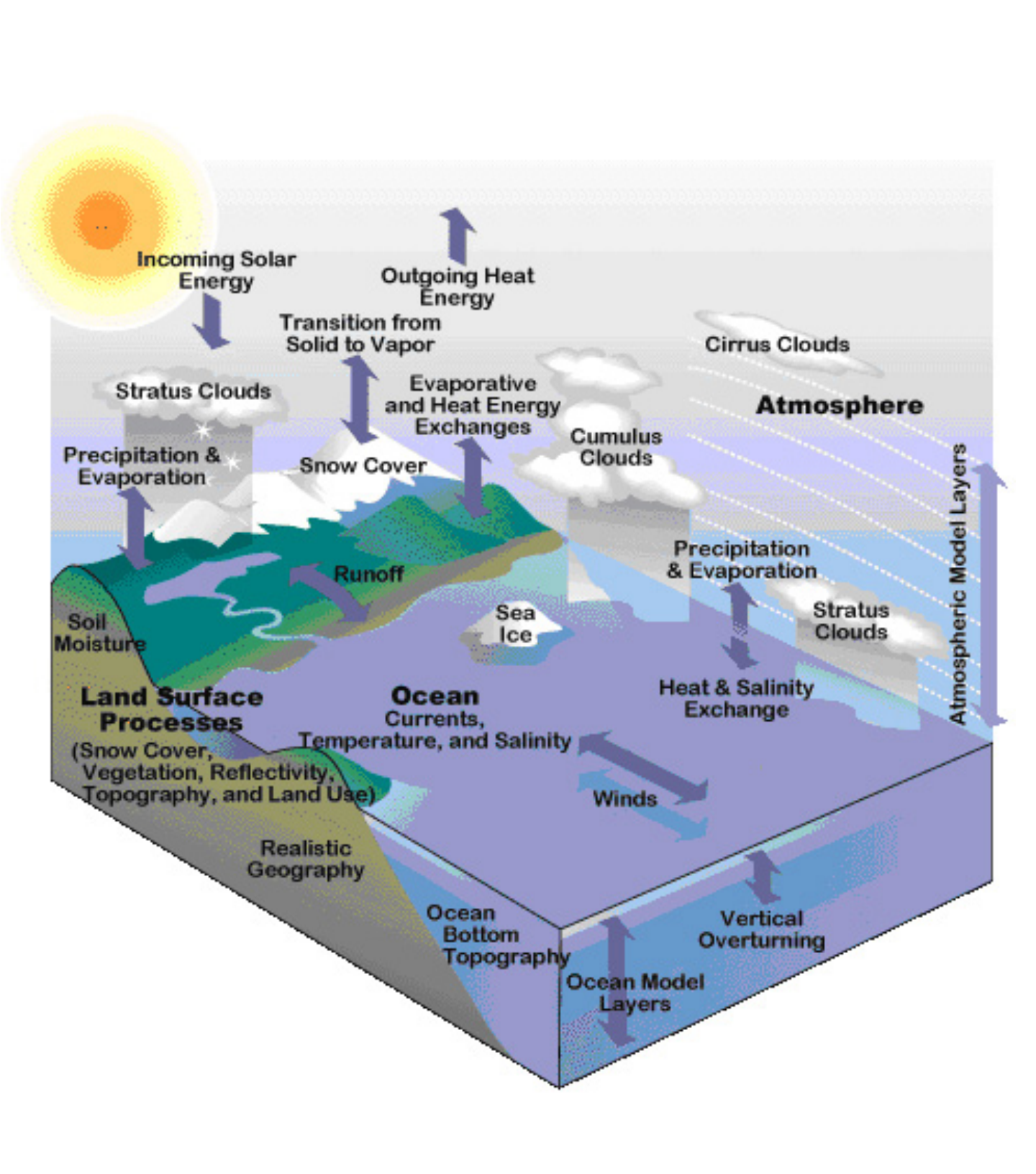
Winds travelling polewards get a bigger and bigger westerly speed (jet streams)

Air becomes unstable

Waves develop in the westerly flow (low pressure systems over Northern Europe)

Mixes warm tropical air with cold polar air

Net transport of heat polewards



Incoming Solar Energy

Outgoing Heat Energy

Transition from Solid to Vapor

Stratus Clouds

Cirrus Clouds

Atmosphere

Precipitation & Evaporation

Evaporative and Heat Energy Exchanges

Cumulus Clouds

Snow Cover

Precipitation & Evaporation

Stratus Clouds

Atmospheric Model Layers

Runoff

Sea Ice

Heat & Salinity Exchange

Soil Moisture

Land Surface Processes

Ocean

(Snow Cover, Vegetation, Reflectivity, Topography, and Land Use)

Currents, Temperature, and Salinity

Winds

Realistic Geography

Vertical Overturning

Ocean Bottom Topography

Ocean Model Layers

Modeling the atmosphere

Lagrangean approach

Conservation of mass:

$$\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} + \frac{\partial w}{\partial p} = 0$$

height is
pressure

Conservation of momentum:

$$\frac{dc}{dt} = \underbrace{-2\Omega \times c}_{\text{Coriolis effect}} - \frac{\text{grad}(p)}{\rho} + \underbrace{\text{grad}(\phi)}_{\text{apparent gravity}} + \underbrace{F}_{\text{friction}}$$

$c=(u,v,w)$; p is geopotential; ρ is density

Material
derivative

$$\frac{\partial}{\partial t} + u \frac{\partial}{\partial x} + v \frac{\partial}{\partial y} + w \frac{\partial}{\partial p}$$

Modeling, cont.

Thermodynamics:

Net heating
rate/unit mass

$$\frac{dT}{dt} = \frac{Q}{c_p} + \kappa \frac{T_w}{p}$$

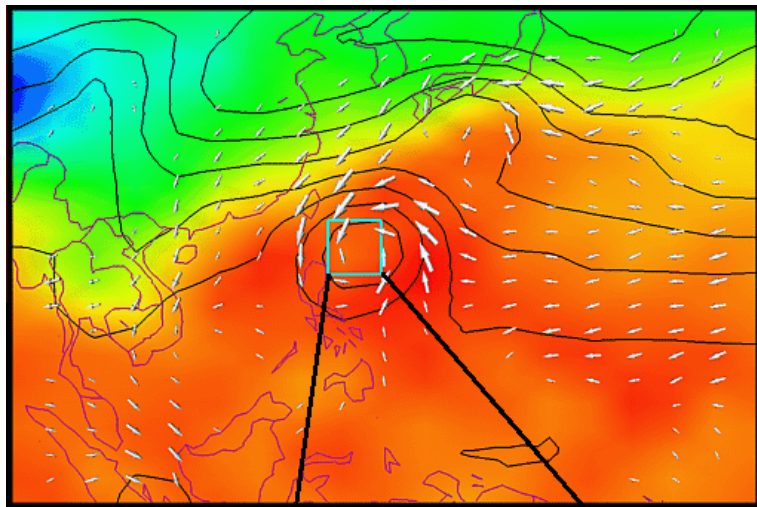
Conservation of water vapor:

$$\frac{dq}{dt} = s(q) + D$$

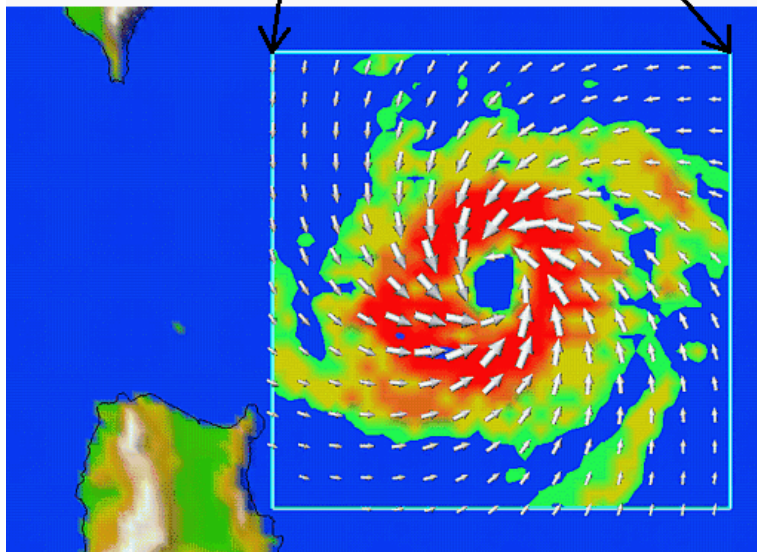
Hydrostatic equilibrium:

$$\frac{\partial \phi}{\partial p} = - \frac{RT}{p}$$

The issue of gridding



Hurricanes
Clouds
Glaciers



Comparing two distributions

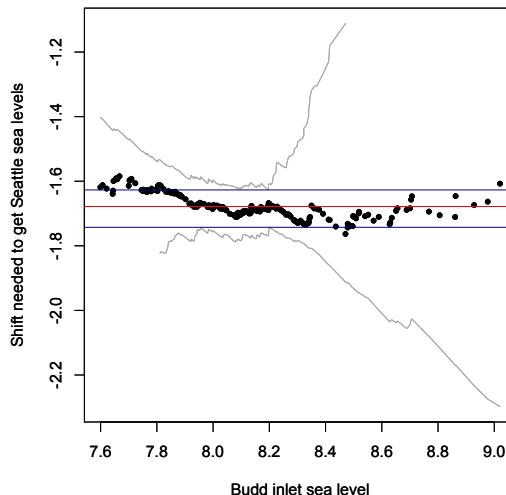
Location shift: $X + \delta \sim Y$

Location-scale: $\alpha X + \delta \sim Y$

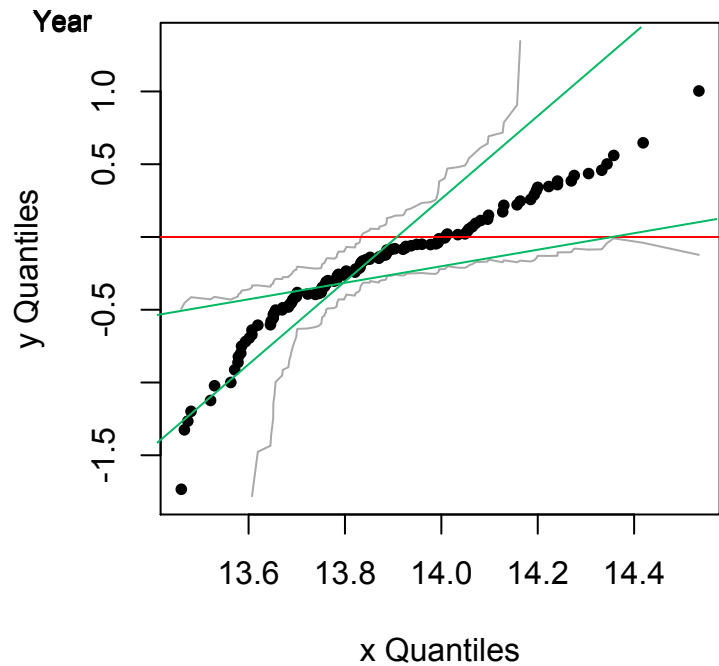
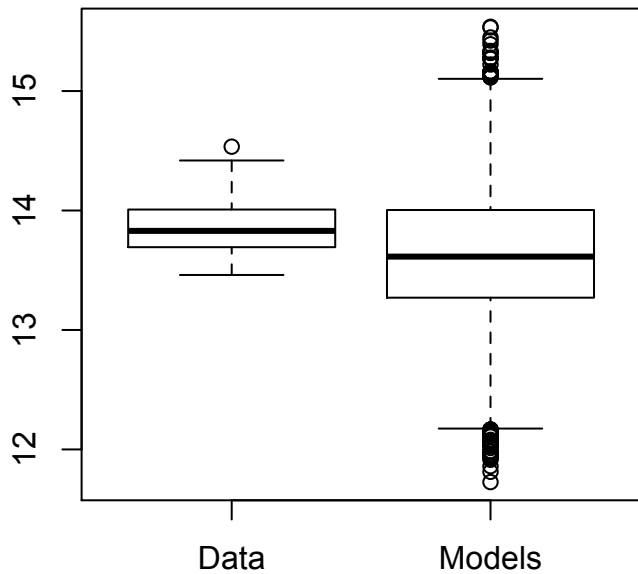
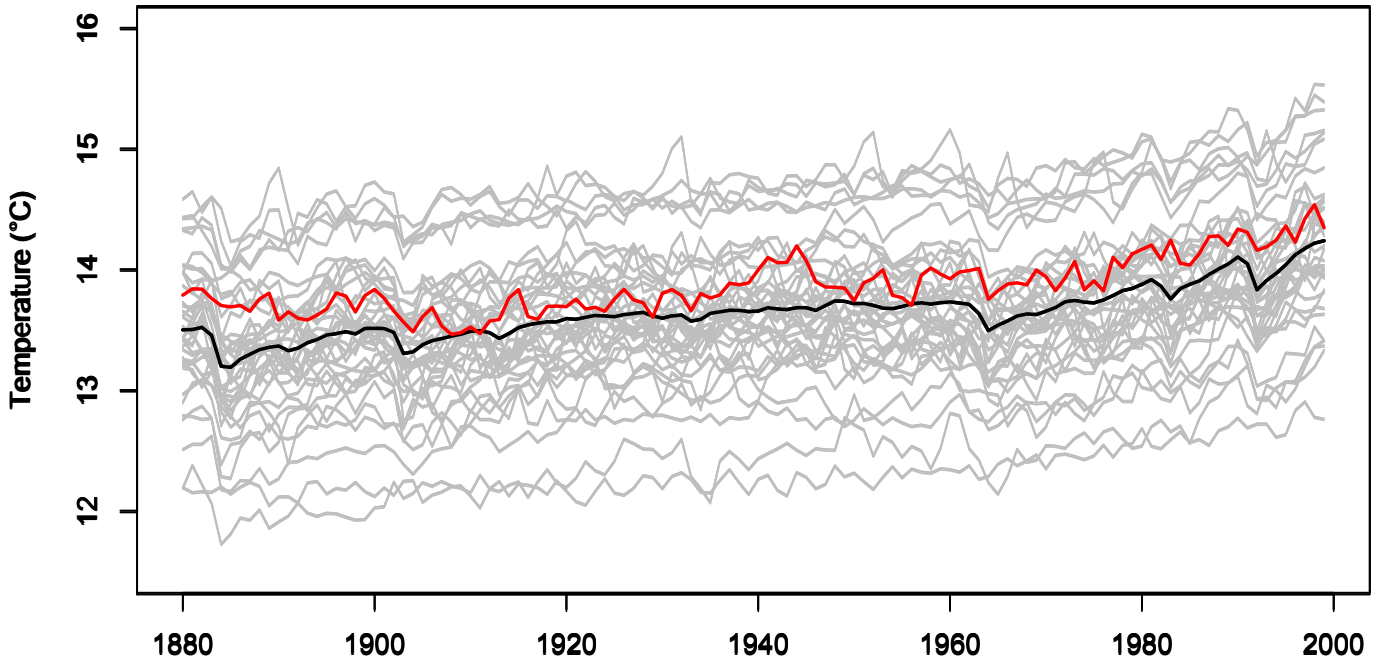
More general: $X + \Delta(X) \sim Y$

Having m observations from Y and n observations from X we estimate

$$\hat{\Delta}(x) = G_m^{-1}(F_n(x)) - x$$



Comparing global climate models to data



Anomalies

Comparison to “normal”

Normal = 30 yr average

Different baselines

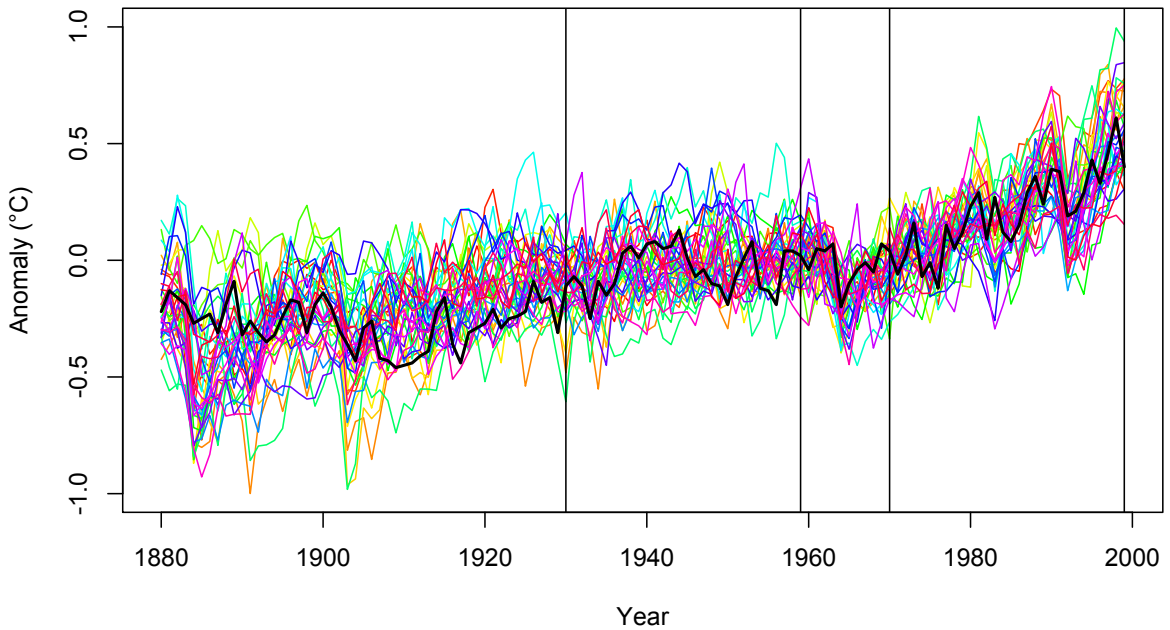
Helps for regional trends

Really residuals

**So fit a model (trend + seasonal +
covariates+variability)**

Global mean temperature

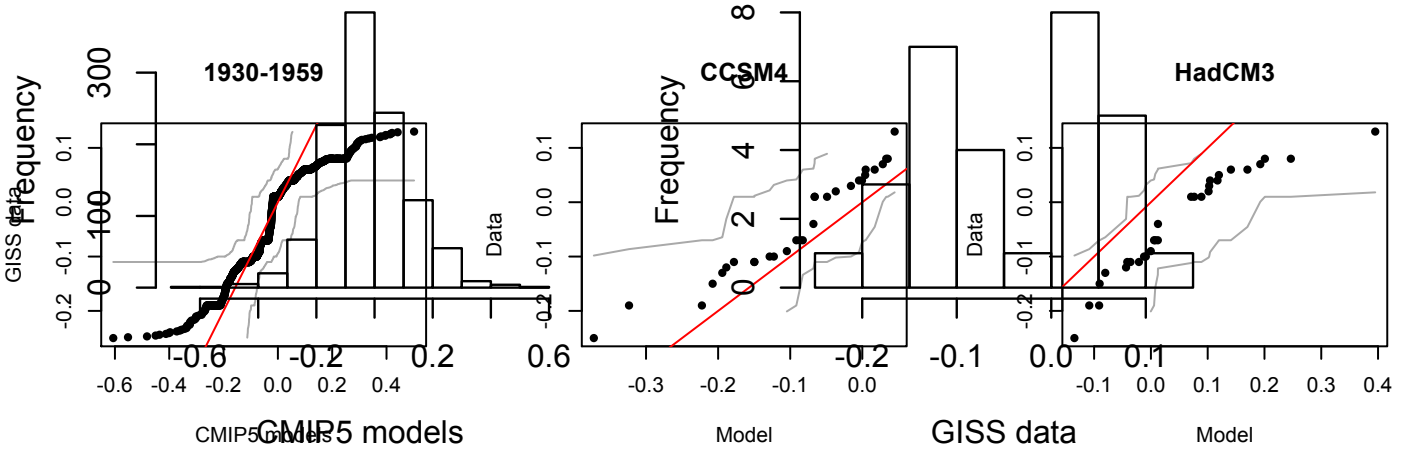
Reference period 1951-1980



30-year distributions

1930-1959

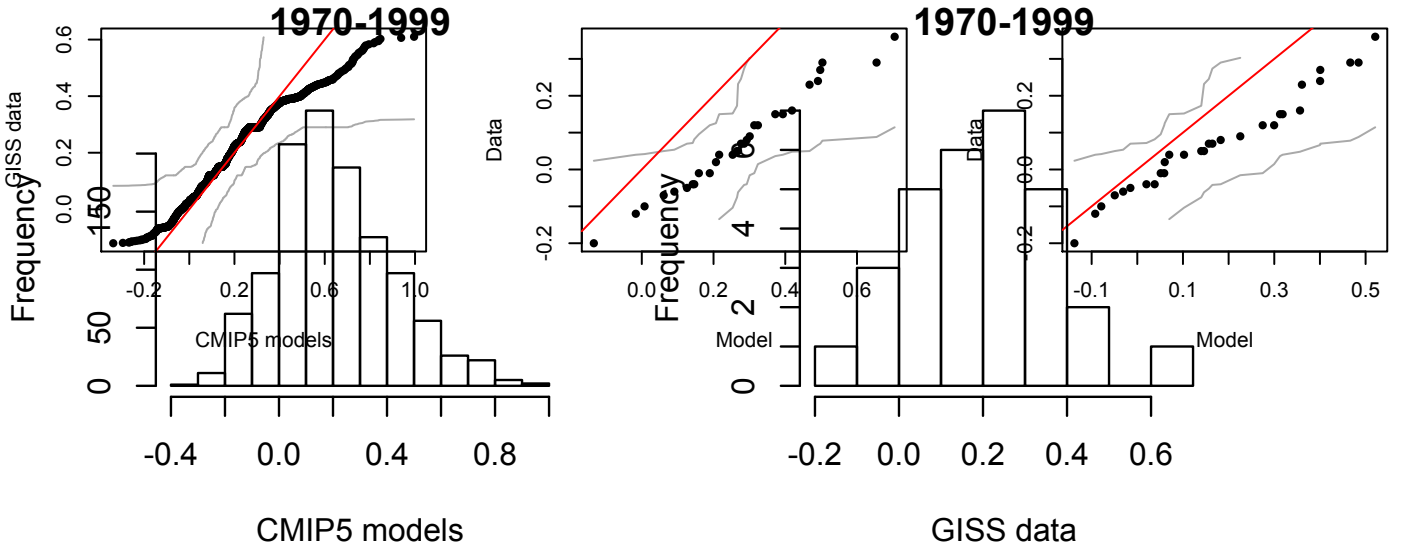
1930-1959



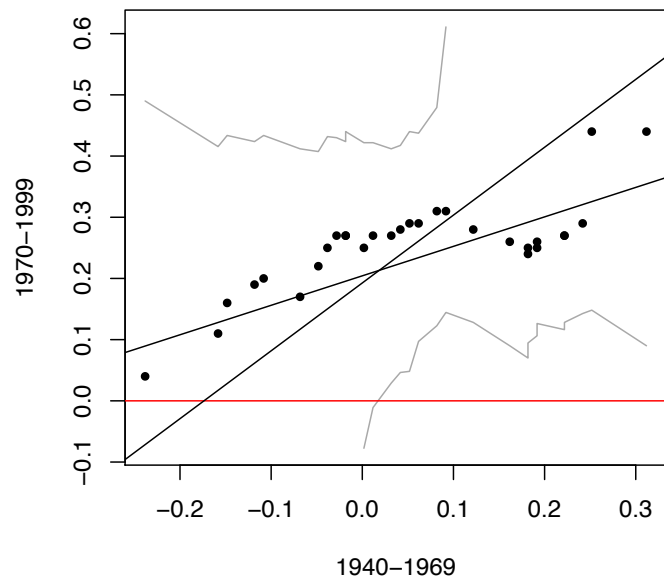
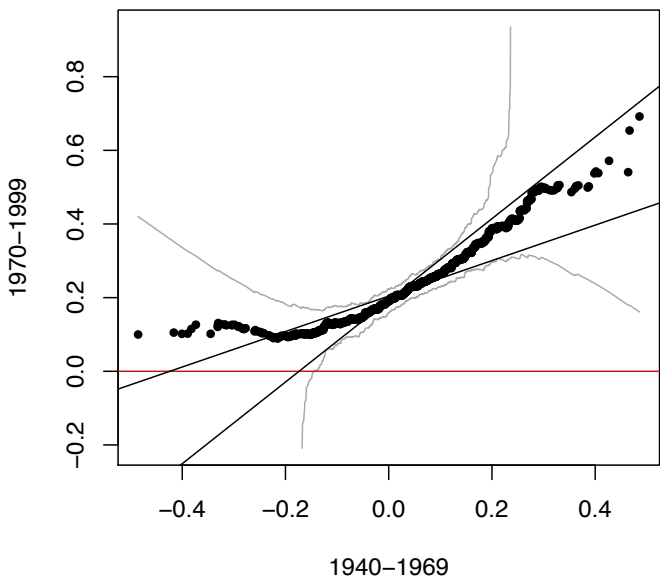
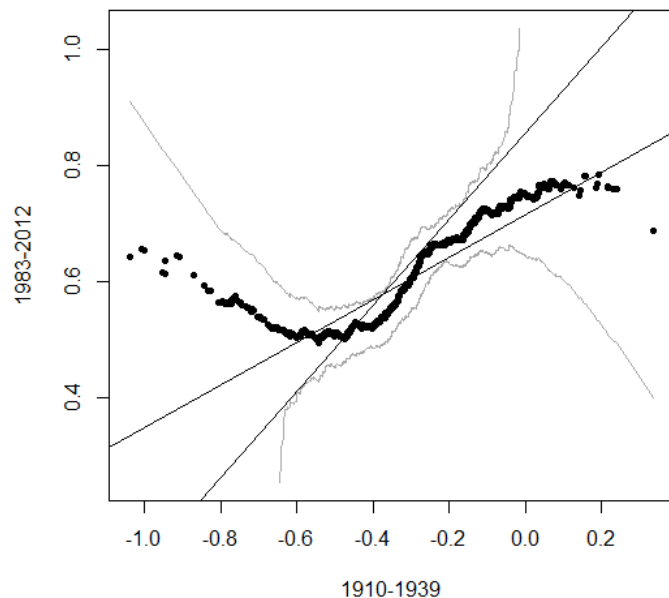
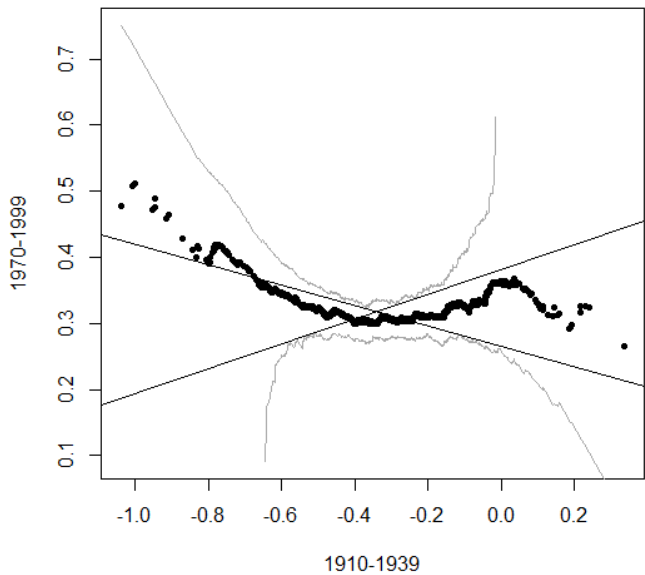
1970-1999

CCSM4

HadCM3

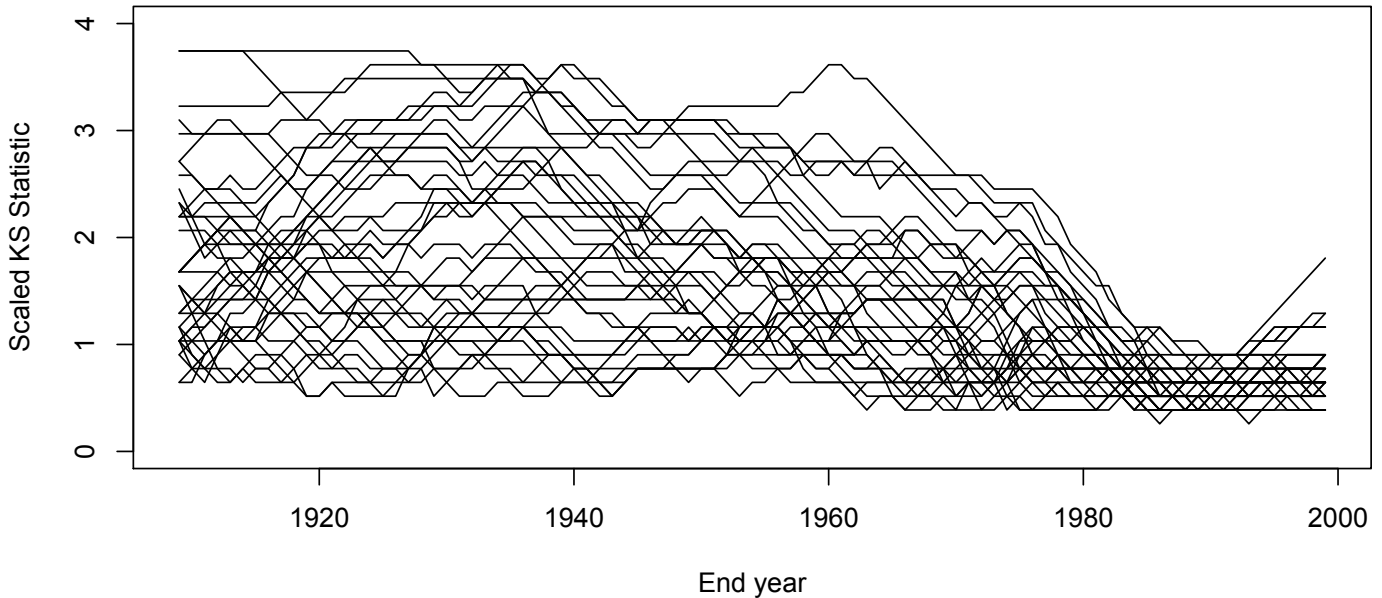


Comparing location and spread

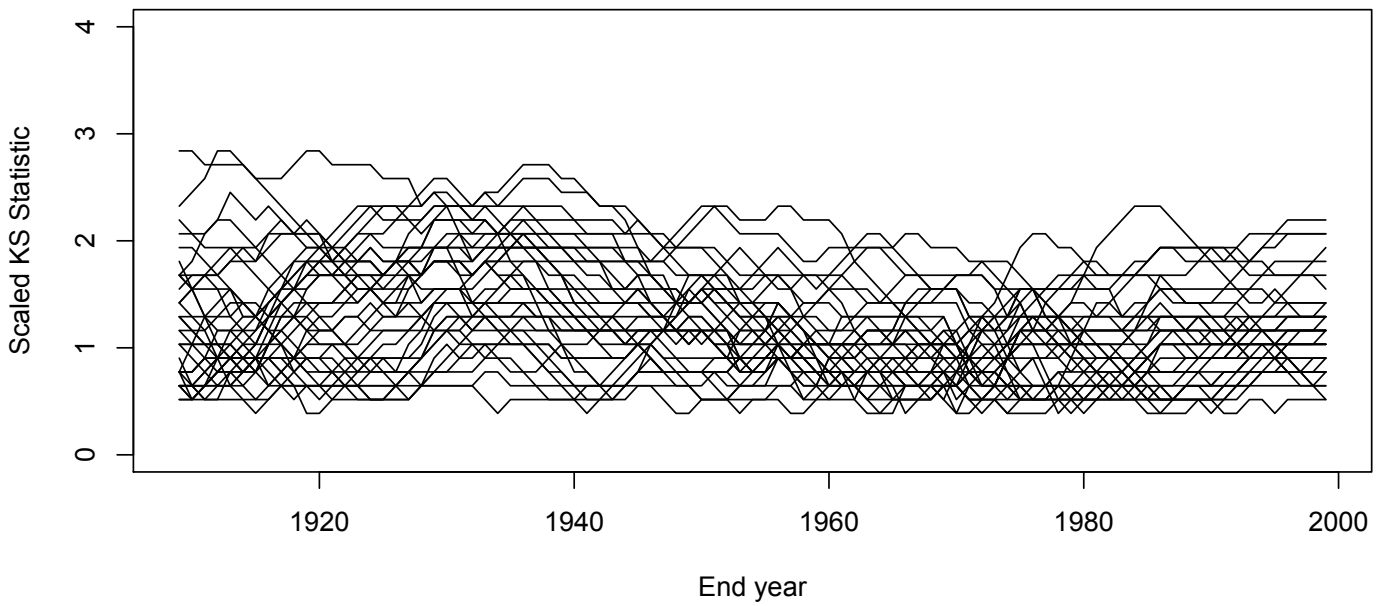


Effect of anomalies

NCEI



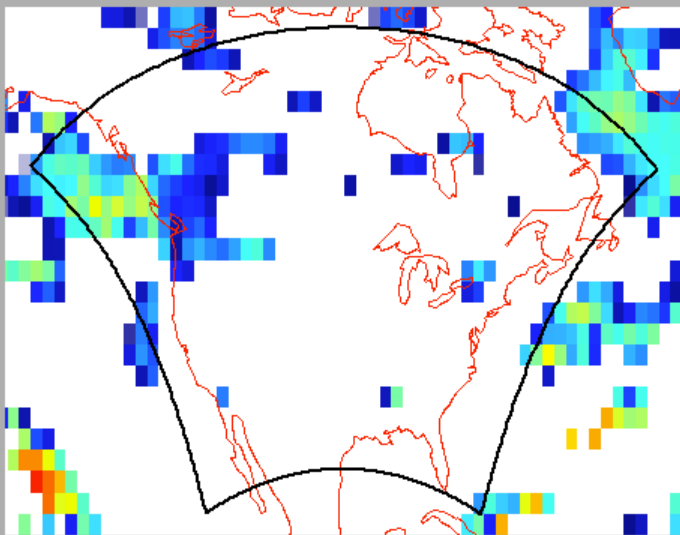
NCEI



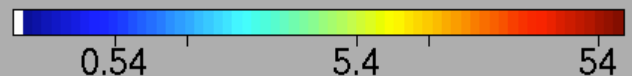
Dynamical downscaling

Global models are very coarse
Regional models are driven by boundary conditions given by global model runs

NCEP reanalysis NARCCAP domain



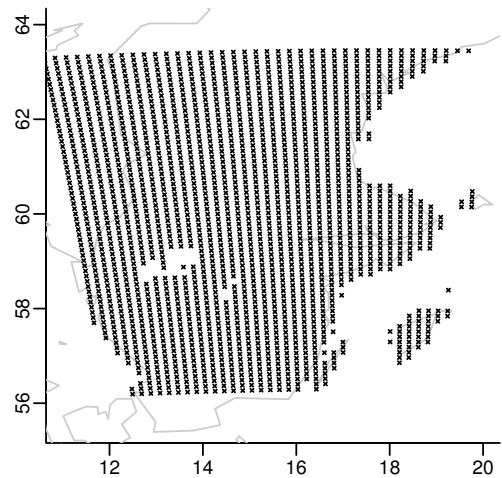
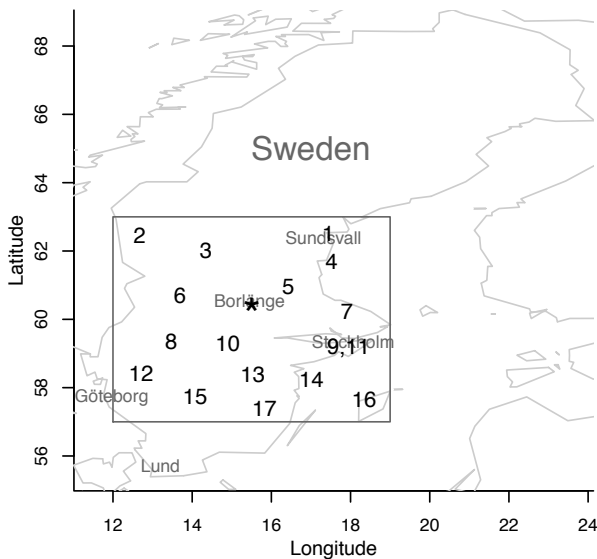
Jan/1/2000 0:00



Swedish temperature minima

SMHI synoptic stations in south central Sweden, 1961-2008. SMHI regional model (open air & snow)

Seasonal minima (d=1 DJF, d=2 MAM, d=3 JJA, d=4 SON).



Spatial models

$$-m_t(\mathbf{s}) \sim \text{GEV}(\mu_t(\mathbf{s}), \sigma(\mathbf{s}), \xi)$$

where

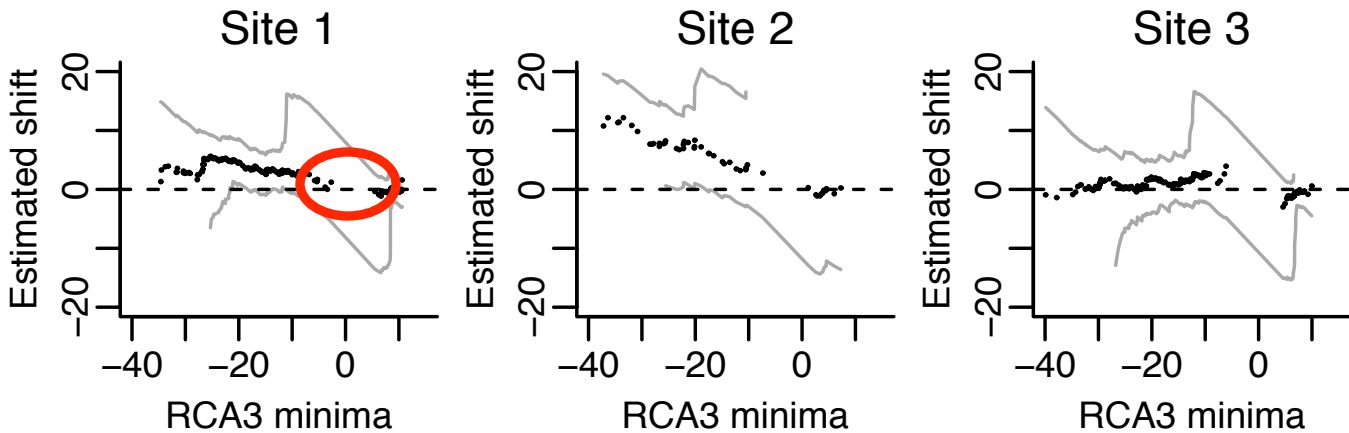
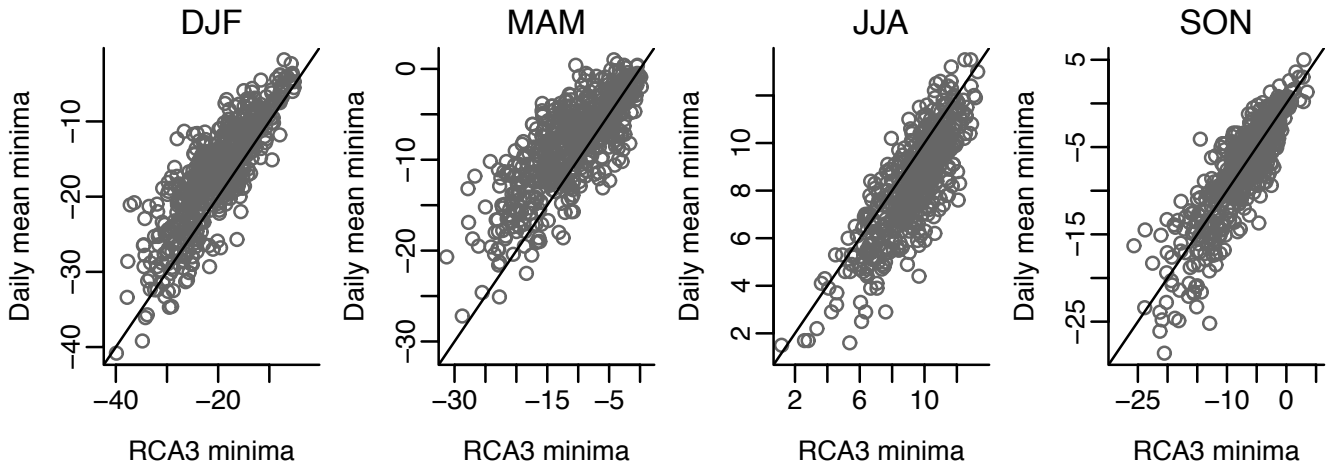
$$\begin{aligned} \mu_t(\mathbf{s}) = & \beta_0(\mathbf{s}) + \beta_1(\mathbf{s})(t - 1961) / 50 \\ & + \sum_{d=2}^4 \beta_d(\mathbf{s}) \mathbf{1}(d_t = d) \end{aligned}$$

$$\beta_i(\mathbf{s}) \sim \text{GP}(\mu_i, \sigma_i(1 - \exp(-\theta_i d(\mathbf{s})))$$

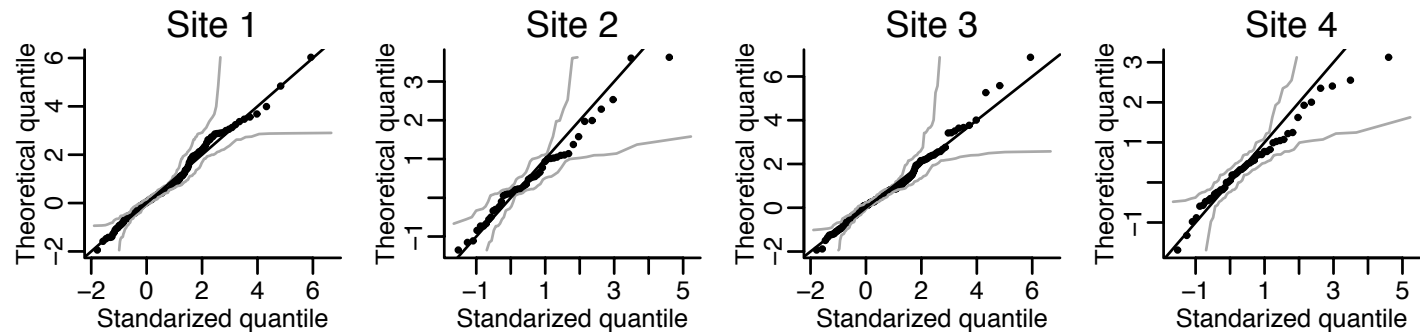
$$\log \sigma(\mathbf{s}) \sim \text{GP}(\mu, \sigma(1 - \exp(-\theta d(\mathbf{s})))$$

Both for data and model output.

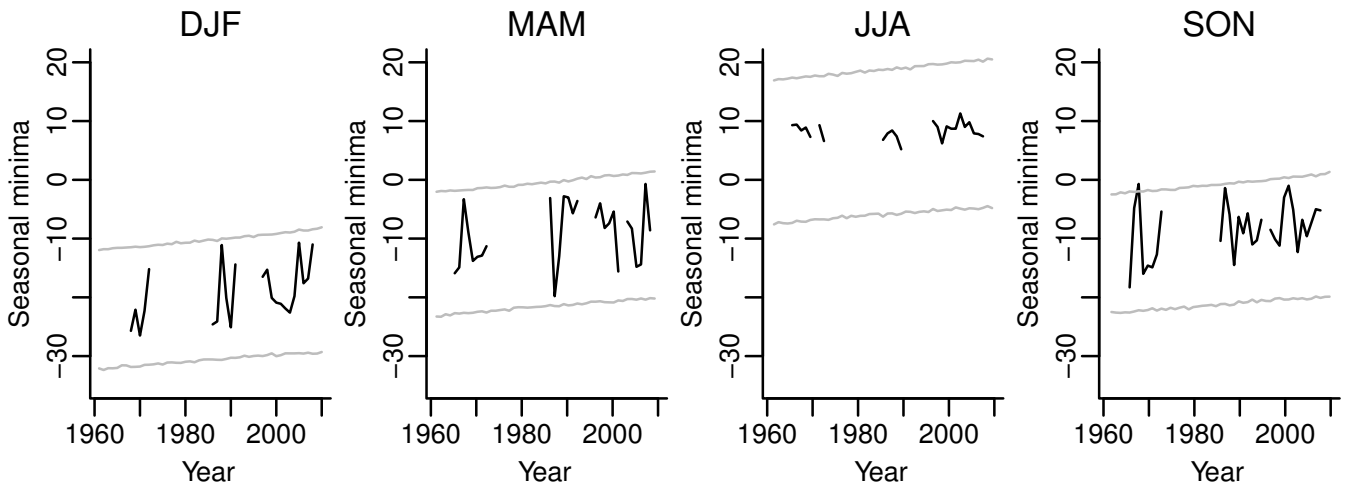
RCM temperature minima



Fit of GEV-distribution



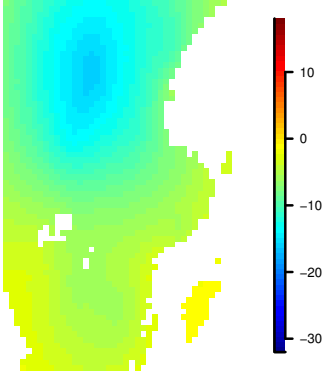
Fit is better when σ depends on s .



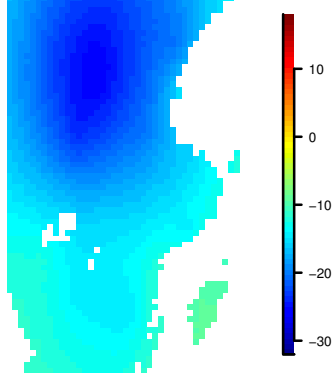
Seasonal fits

Obs. Stations

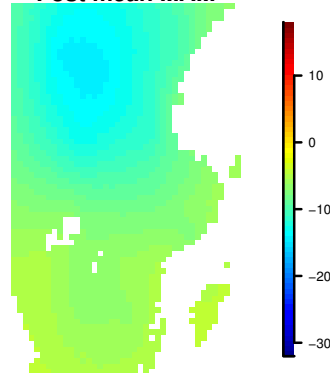
Post mean SON



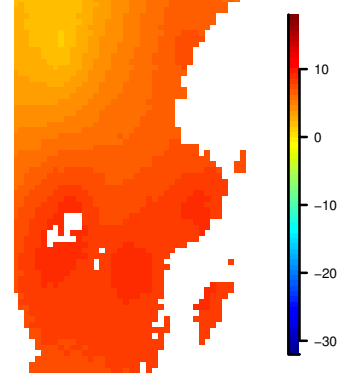
Post mean DJF



Post mean MAM

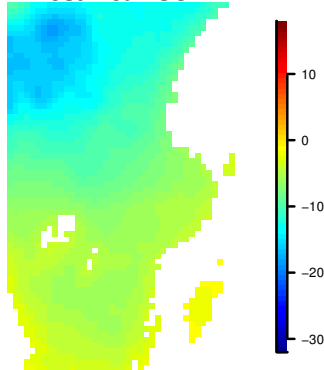


Post mean JJA

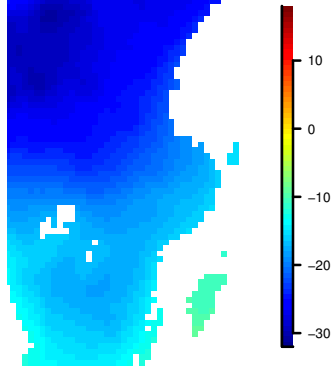


RCM

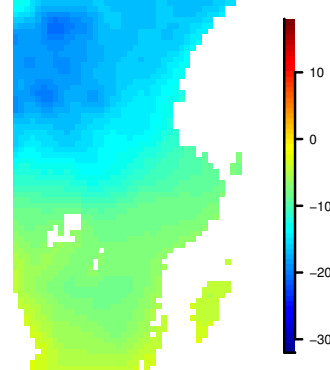
Post mean SON



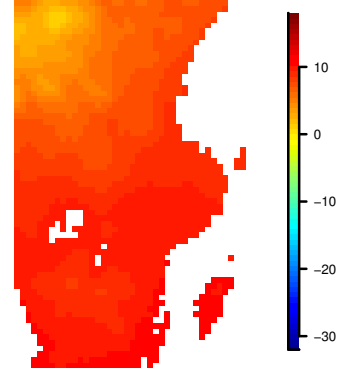
Post mean DJF



Post mean MAM



Post mean JJA

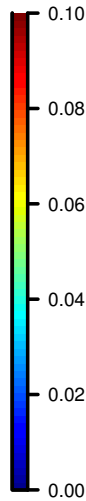
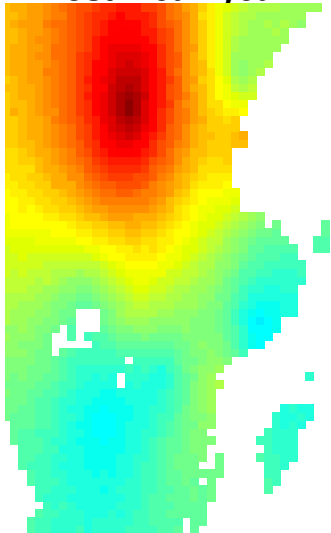


Trend fits

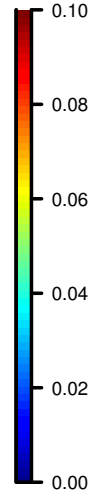
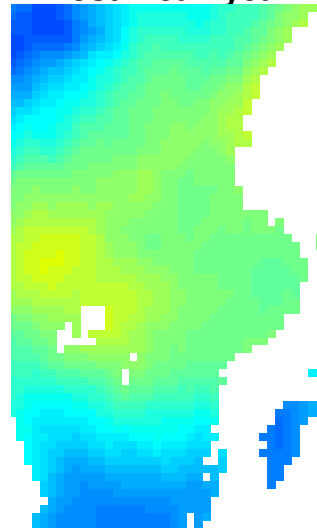
Observed stations

RCM

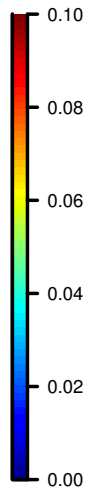
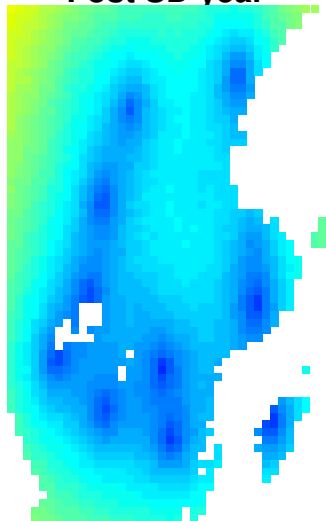
Post mean year



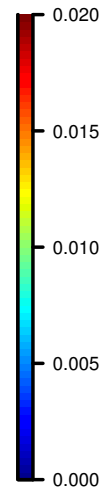
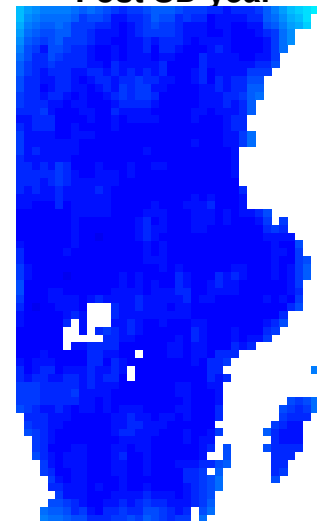
Post mean year



Post SD year



Post SD year



(Dis)agreement between RCM and data

Seasonal effects quite similar

Similar spatial scale

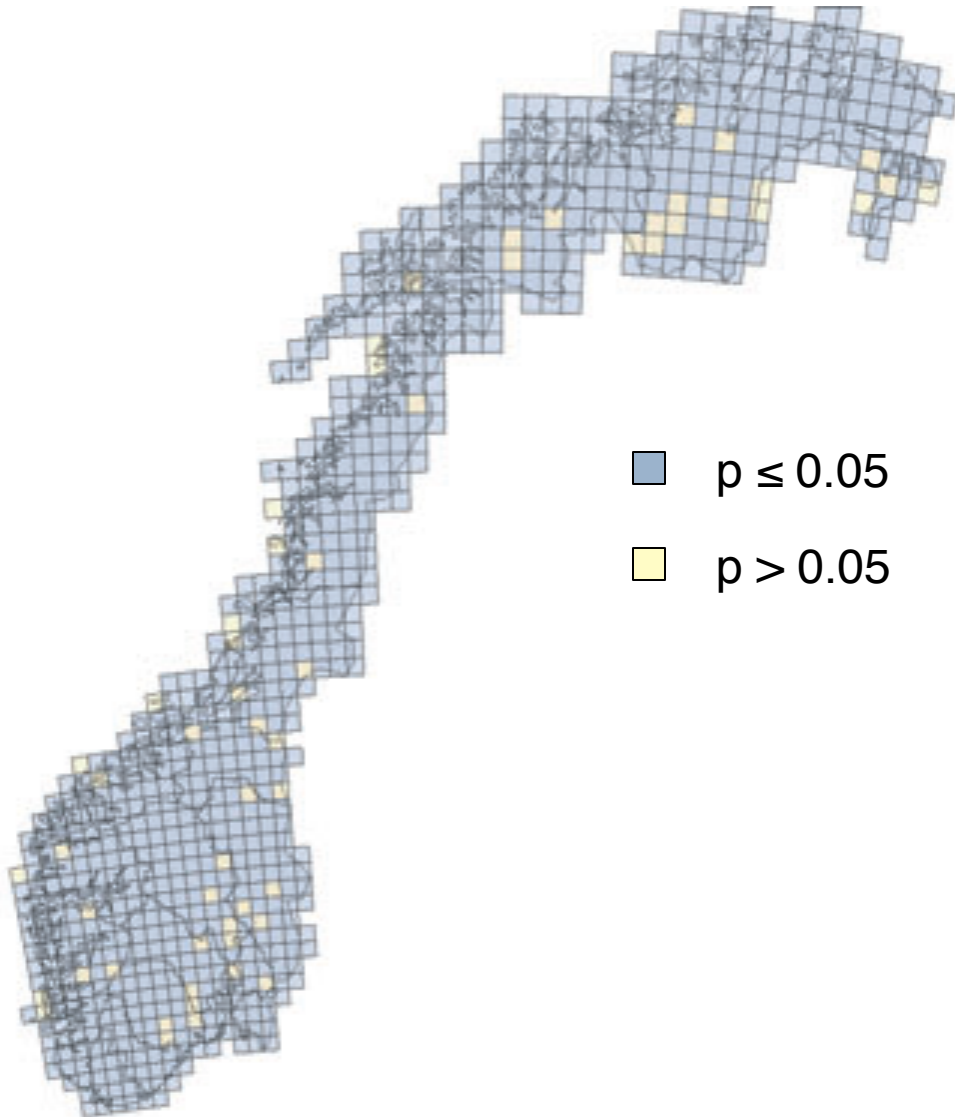
Similar shape parameter

**Temporal trend substantially
lower in model output**

Data trend about 0.4-1°C /decade

(lower than the annual model)

Norwegian winter precip



Bias correction

Need downscaled precipitation projections for adaptation plans

Bias correction for downscaled reanalysis

Apply to downscaling historical GCM

If works, apply to downscaling GCM projections

Correction more important for large quantiles than for entire distribution

Full quantile correction

Applying the Doksum shift we get

$$\begin{aligned}z_{it'}^{\text{cal}} &= z_{it'}^H + \hat{\Delta}_i(z_{it'}^H) \\ &= z_{it'}^H + \hat{G}_i^{-1}(\hat{F}_i(z_{it'}^H)) - z_{it'}^H \\ &= \hat{G}_i^{-1}(\hat{F}_i(z_{it'}^H))\end{aligned}$$

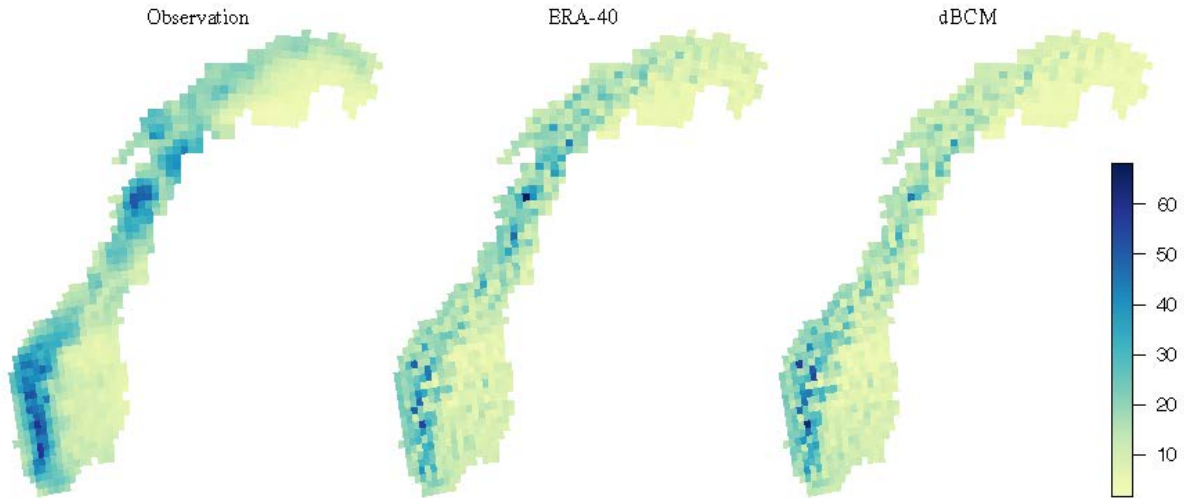
Rejections (fit to 80%, tested on 20%):

Raw 77%

Corrected 18%

Corrected GCM 79%

Single quantile correction

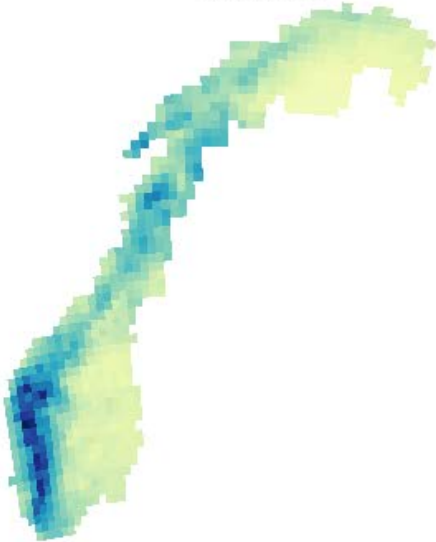


$$\log(Y^q) = \alpha + \text{diag}(\log(X^q))\beta + \varepsilon$$
$$\beta \sim \text{GP}(0, \Sigma(\nu, \kappa, \phi))$$

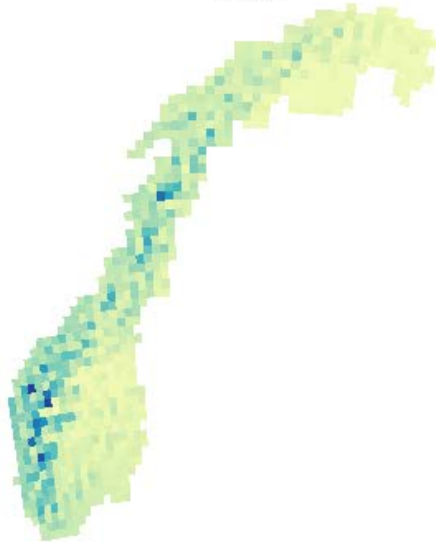
Replace with
smoothed version

Bias-correction of 95th precipitation percentile

Observation



dBCM



Calibrated dBCM

